



POLITECNICO | DIPARTIMENTO
MILANO 1863 | DI MATEMATICA

Digital Twins in Computational Oncology: Probabilistic Formulation of Personalized Risk Assessment

Francesca Arceci - MOX, Department of Mathematics, PoliMi

Joint work with

Prof. Paolo Zunino, Dr. Piermario Vitullo, MOX, DMAT, PoliMi

CMON Lab, Data Science Unit, Fondazione IRCCS Istituto Nazionale dei Tumori

20-24.11.2025 | Workshop

"The Mathematics of Scientific Machine Learning and Digital Twins"

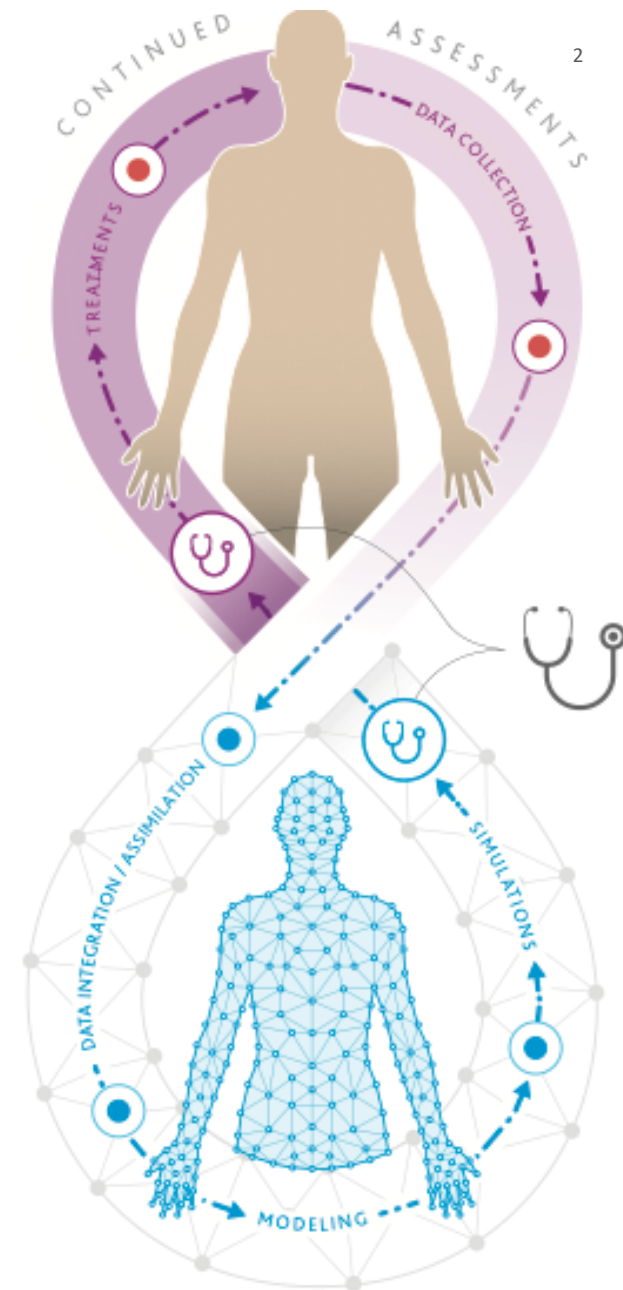
Digital Twin in Oncology

Radiation therapy (RT) is commonly used after surgery for various types of cancer, including **breast cancer**.

Despite protection and safety measures, radiation therapy can expose the lung and heart to radiation, **raising the risk of severe cardiac and pulmonary diseases**.

The project TETRIS proposes to explore the opportunities and challenges of applying **digital twins (DTs)** in RT safety.

What is a digital twin?



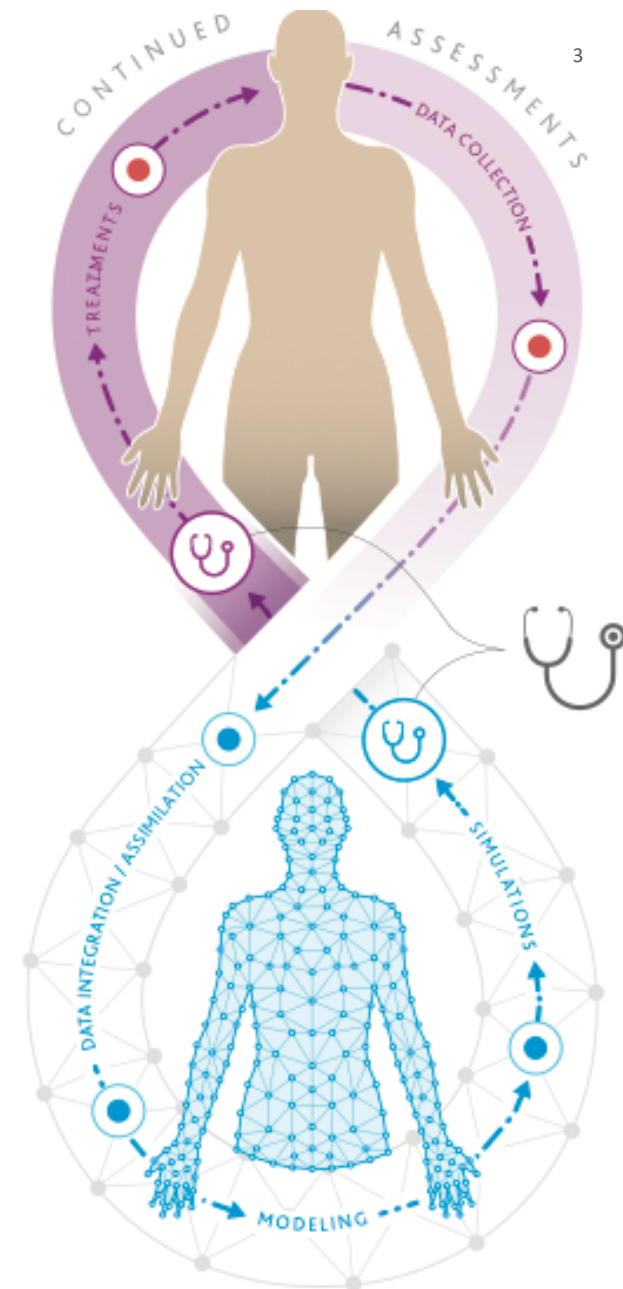
Risk assessment **T**ools for severe side **E**ffects after **breasT** Radiotherapy:
radiation safety through biological extended models and **d**igital twin**S**



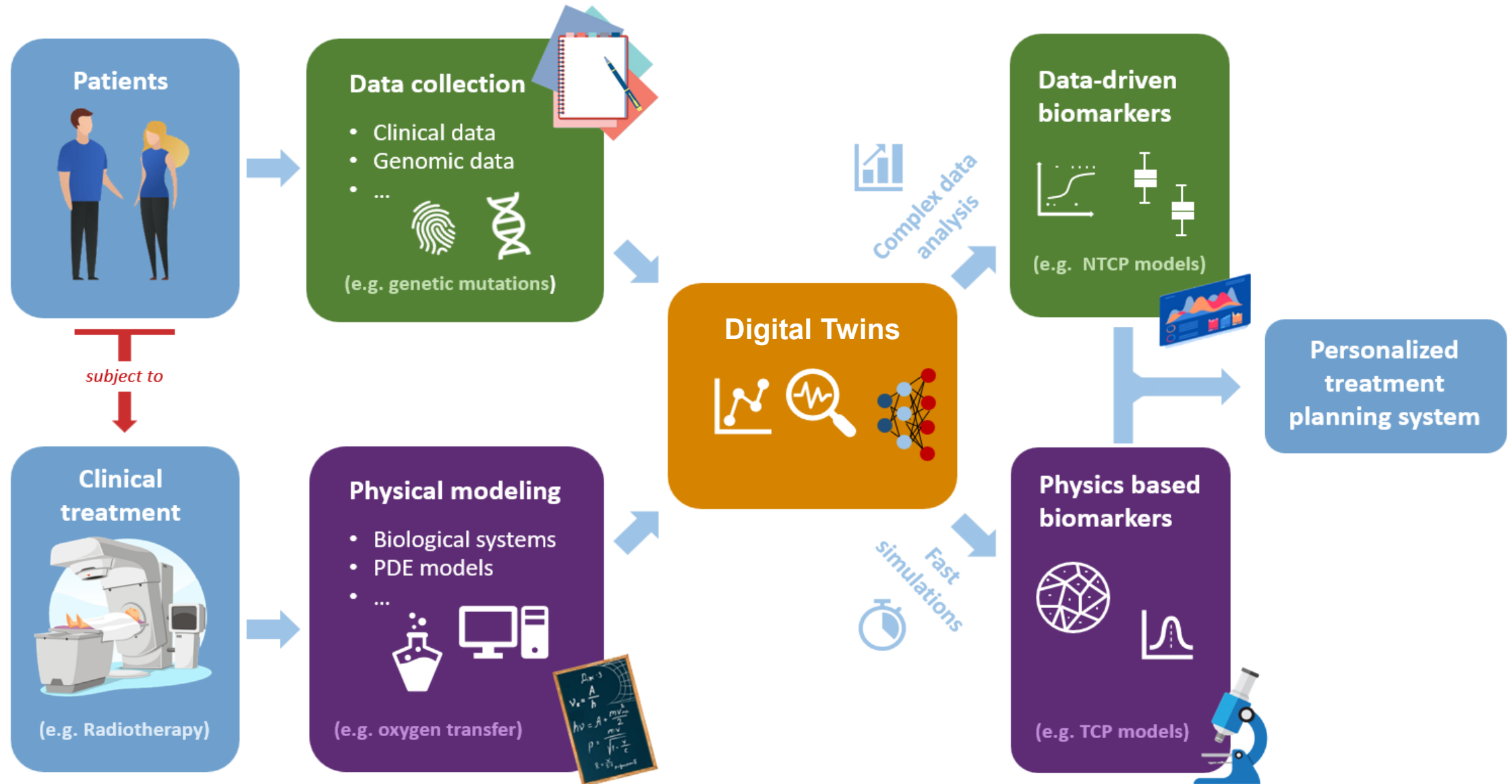
Digital Twin in Oncology

What is a digital twin?

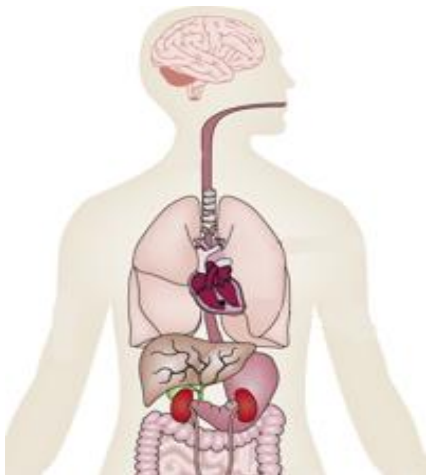
- A digital twin is a set of **virtual information constructs** that mimics **structure, context, and behaviour** of a physical system.
- A digital twin is **dynamically updated** with real-time **data** from its physical twin.
- A digital twin has **predictive capabilities**.
- It informs **decision-making that realize value**
- The **bidirectional interaction** between the virtual and the physical is central to the digital twin.



Digital Twins for Computational Oncology

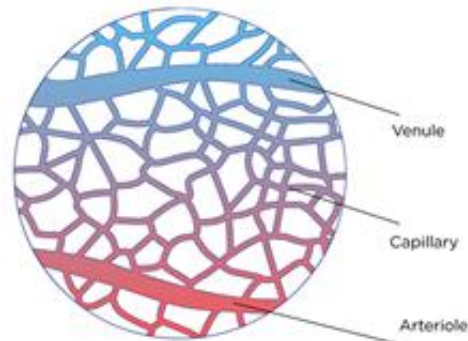


Personalized Radiotherapy



Personalize the treatment at the patient level to **maximize** the chances of **tumor eradication** and **prevent late toxicity**.

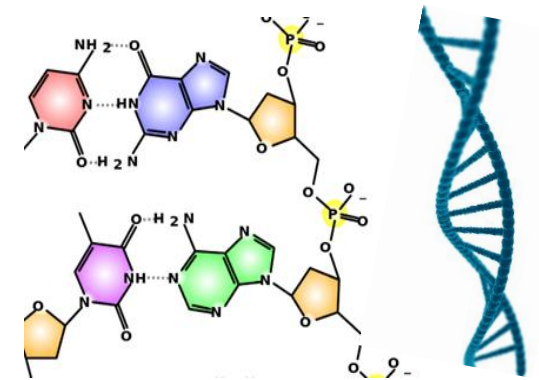
Physics driven



- How does the **tumoral micro-environment** affect radiotherapy?
- Can we provide **robust** and **efficient** numerical simulations?

Personalized
Treatment
Planning

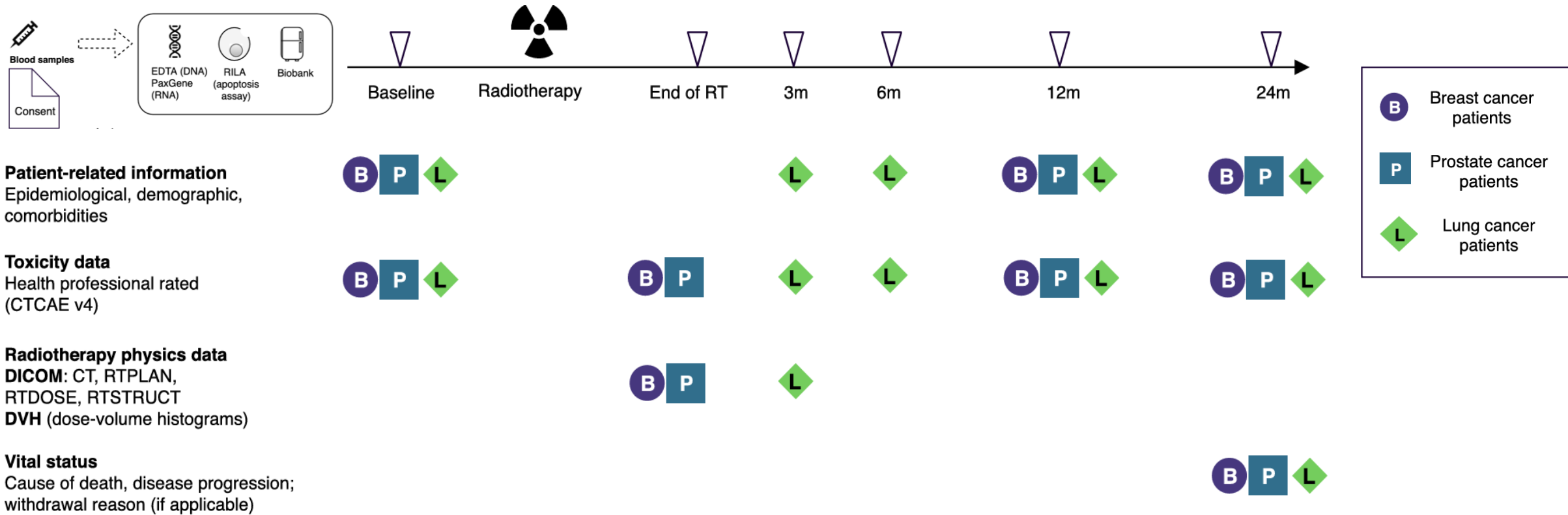
Data driven



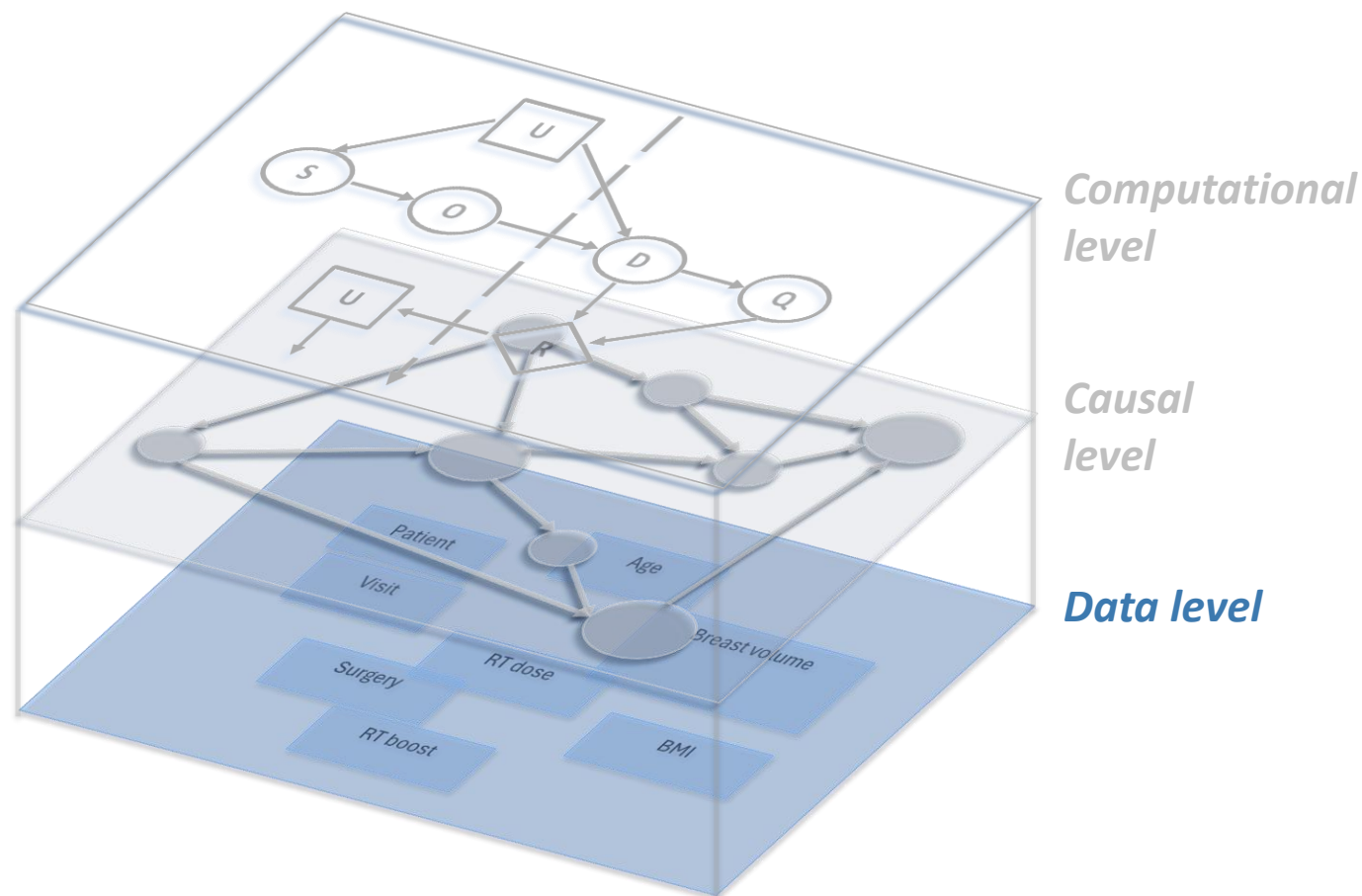
- Can we quantify the risk?
- How do **genetic** traits influence radiosensitivity?

The REQUITE dataset

REQUITE is a large, international, multi-center cohort comprising over 5000 patients treated for breast, prostate, or lung cancer (*Seibold, Petra et al. Radiotherapy and Oncology, Volume 138, 59 – 67*).

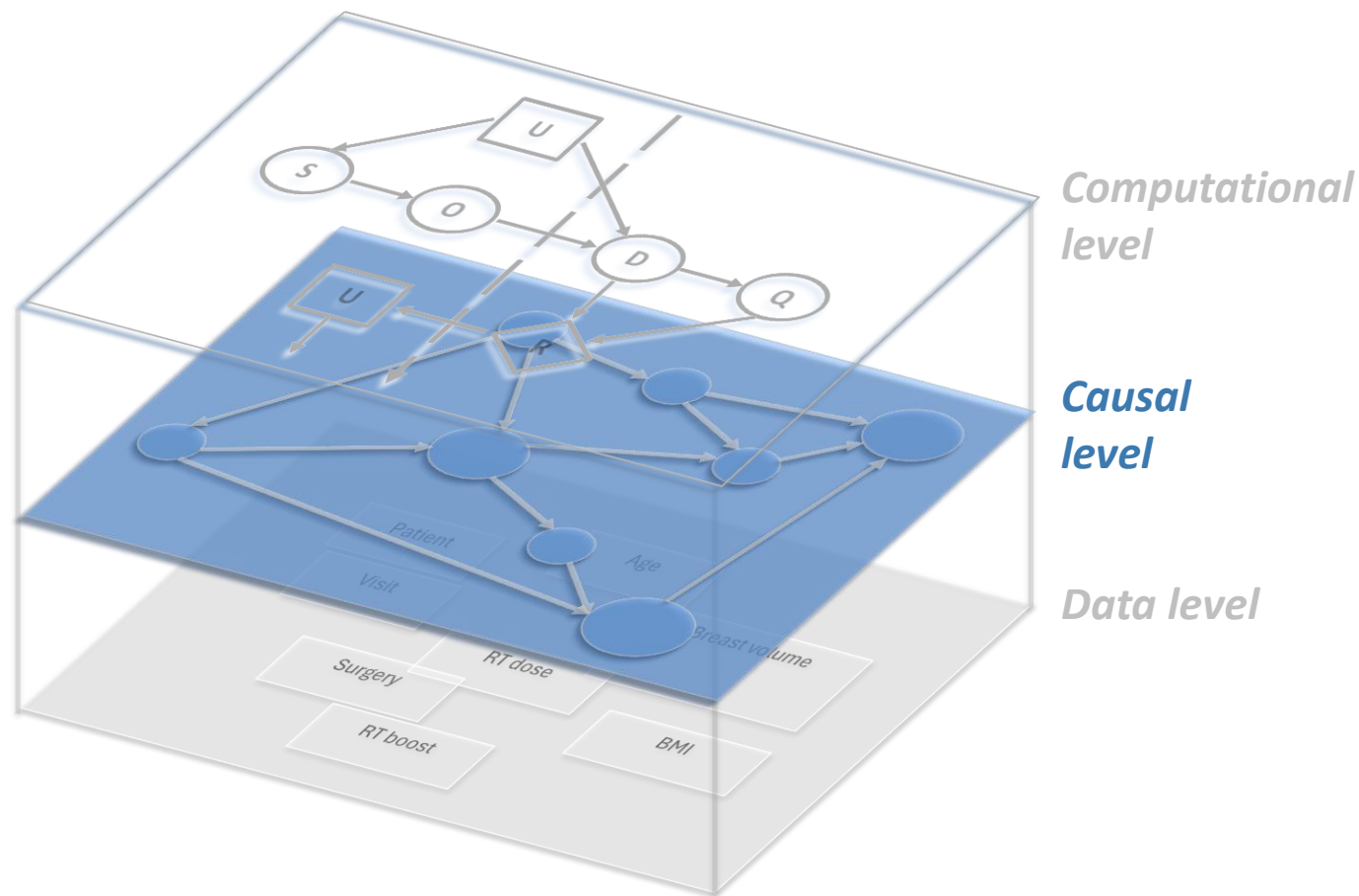


Towards the the DT for breast cancer patients



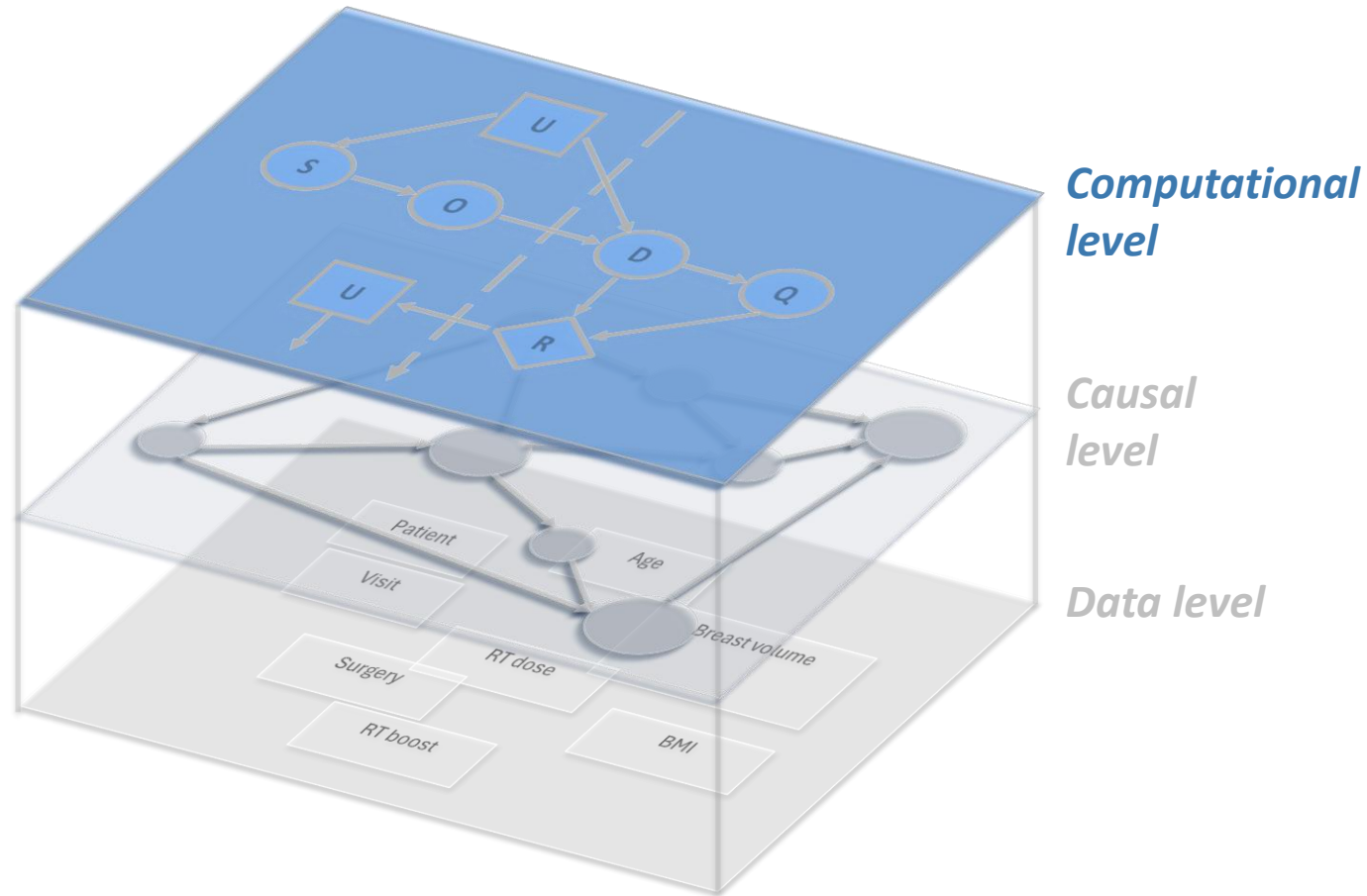
Seibold, Petra et al., *REQUIRE: A prospective multicentre cohort study of patients undergoing radiotherapy for breast, lung or prostate cancer*, Radiotherapy and Oncology, Volume 138, 59 – 67 (2019)

Workflow for breast cancer patients



van Amsterdam WAC et al., *Causal Inference in Oncology: Why, What, How and When*, Clinical Oncology, Volume 38 (2025)

Workflow for breast cancer patients

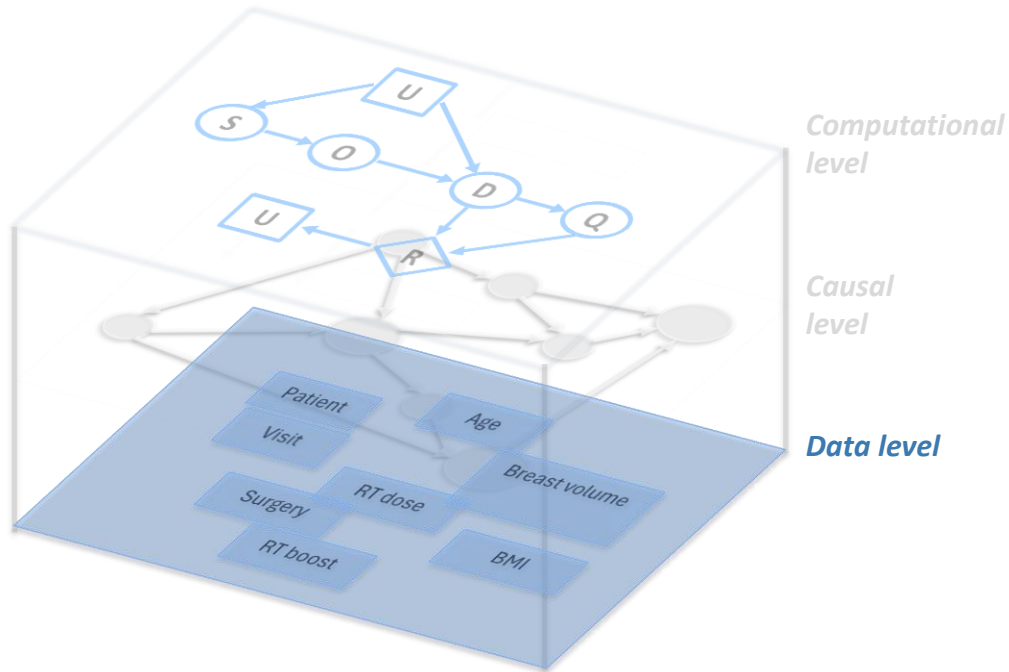


Willcox K.E. et al., *A probabilistic graphical model foundation for enabling predictive digital twins at scale*, Nature Computational Science, 1 (5), pp. 337 – 347 (2021)

Breast cancer patients: data level

The breast dataset consists in 2057 patients.

Data available up to 24 months after RT.



Patient information:

- **Clinical data:** Age, BMI, comorbidities
- **Genomic data:** SNP genotypes, polygenic risk scores
- **Imaging data:** DICOM-RT

[B2a Breast patient factors baseline 2025-05-16 18-28-34.xlsx](#)

Breast toxicity data:

- Nipple retraction
- Skin induration (fibrosis)
- Erythema
- Pneumonitis

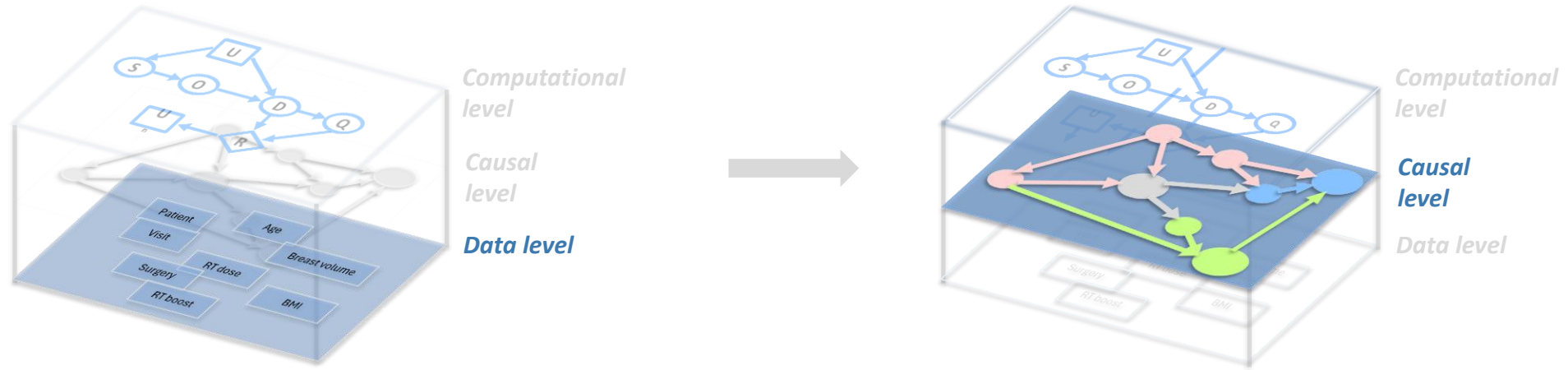
[B5 Health professional 2025-05-16 18-31.xlsx](#)

Breast clinical and treatment information:

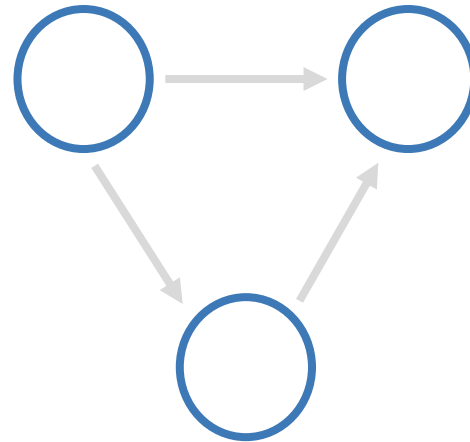
- RT prescribed dose, fraction dose
- Breast skin dose, heart mean dose, lung mean dose
- RT boost, photon boost, neoadjuvant

[B3 Breast clinical and treatment data form 2025-05-16 18-30-19.xlsx](#)

Breast cancer patients: causal level



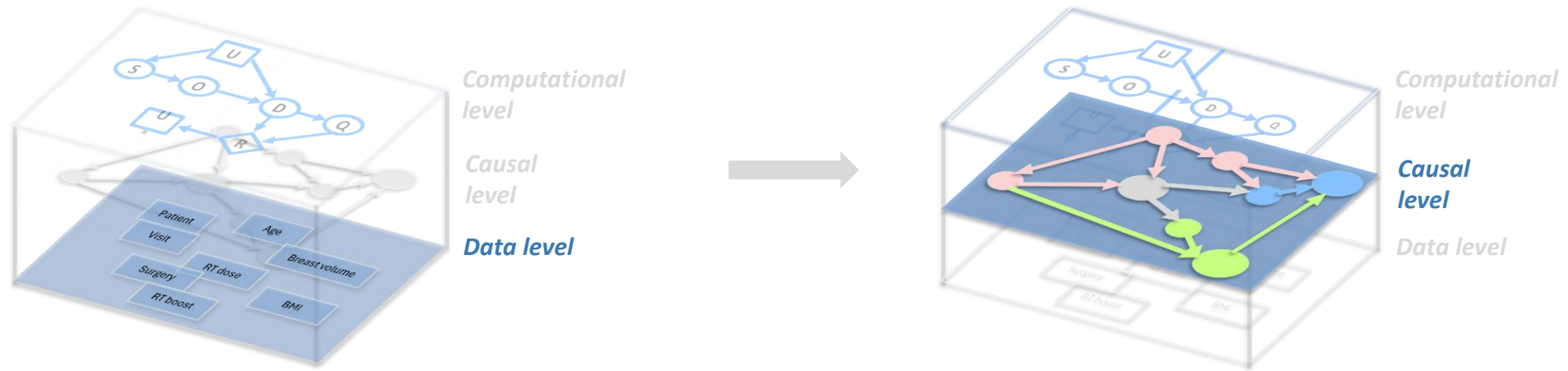
- **Predictive models** not necessarily focus on the relationships among variables
- **Causal inference models** to uncover the mechanisms behind observed phenomena



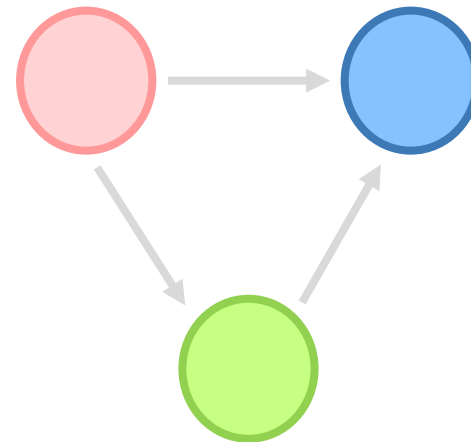
Directed Acyclic Graphs

- ❖ **Nodes:** *selected variables*
- ❖ **Arrows:** *relationships from cause to effect*

Breast cancer patients: causal level

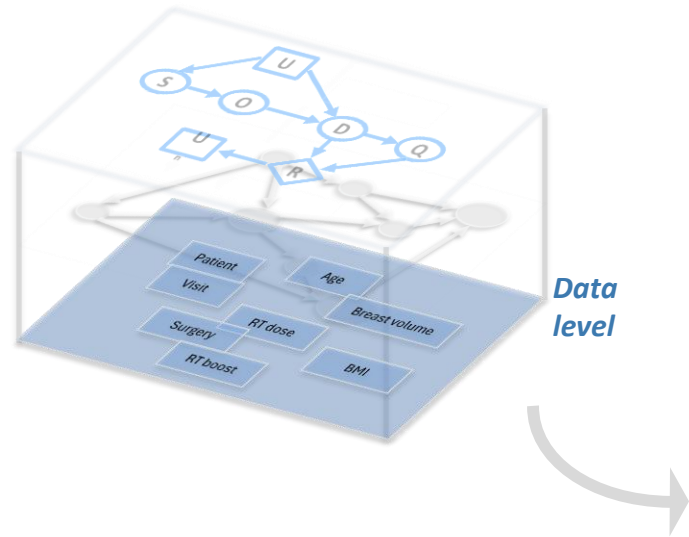


- **DAG** wants to explore the **direct effect** of the **exposure** on the **outcome**
- **Confounding variables** affect both the exposure and the outcome

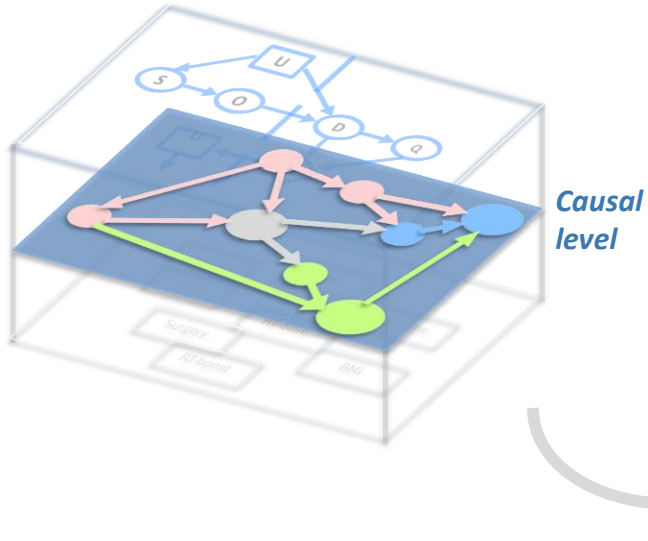


- ❖ **Exposure variable**
- ❖ **Outcome variable**
- ❖ **Confounding variable**

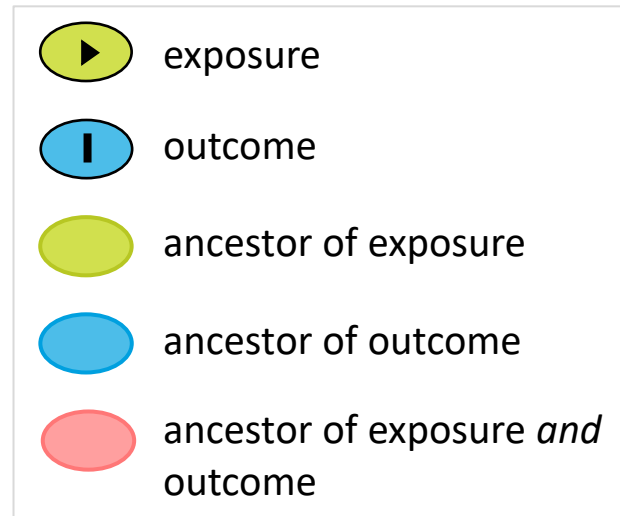
Causal model



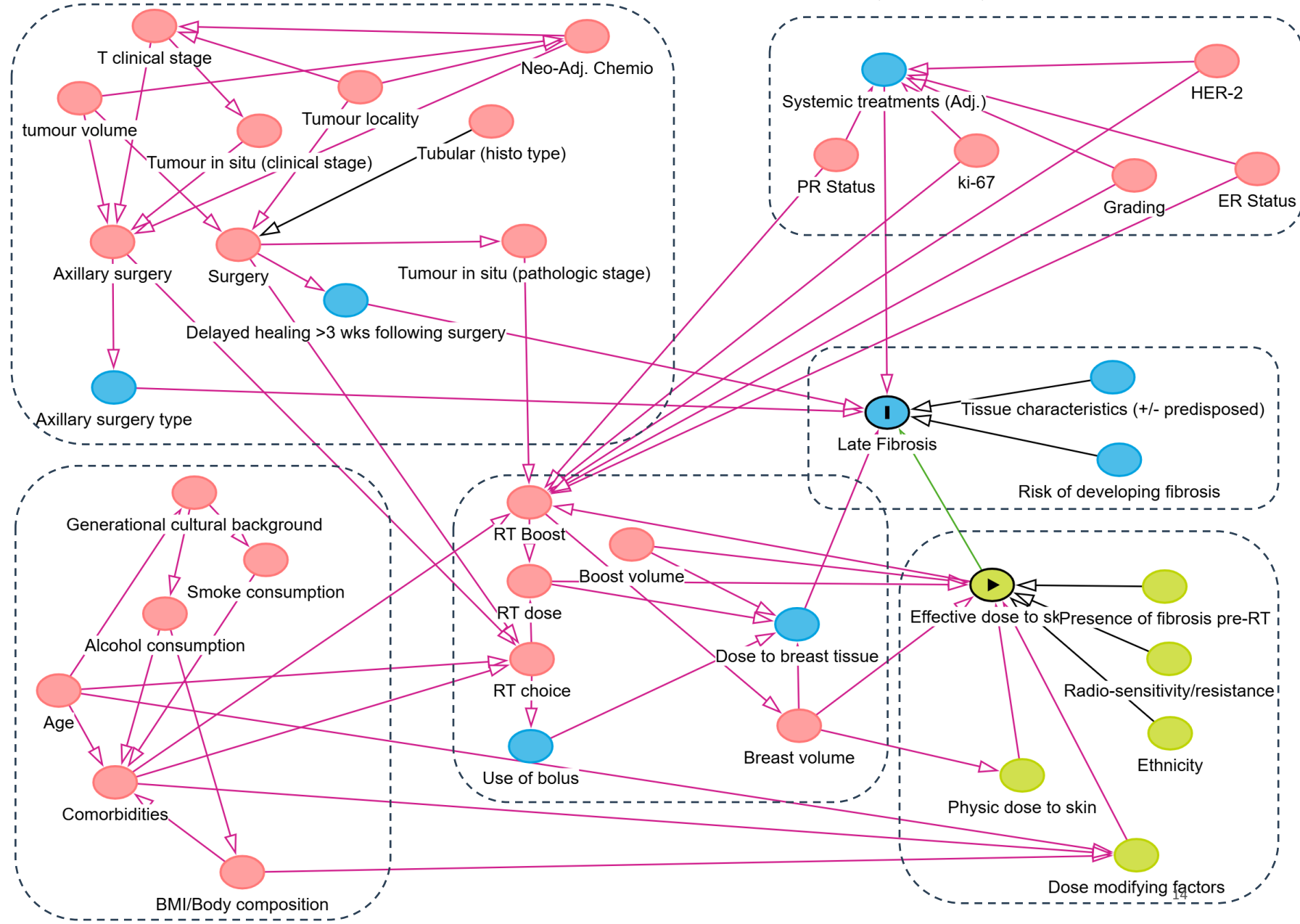
Causal model



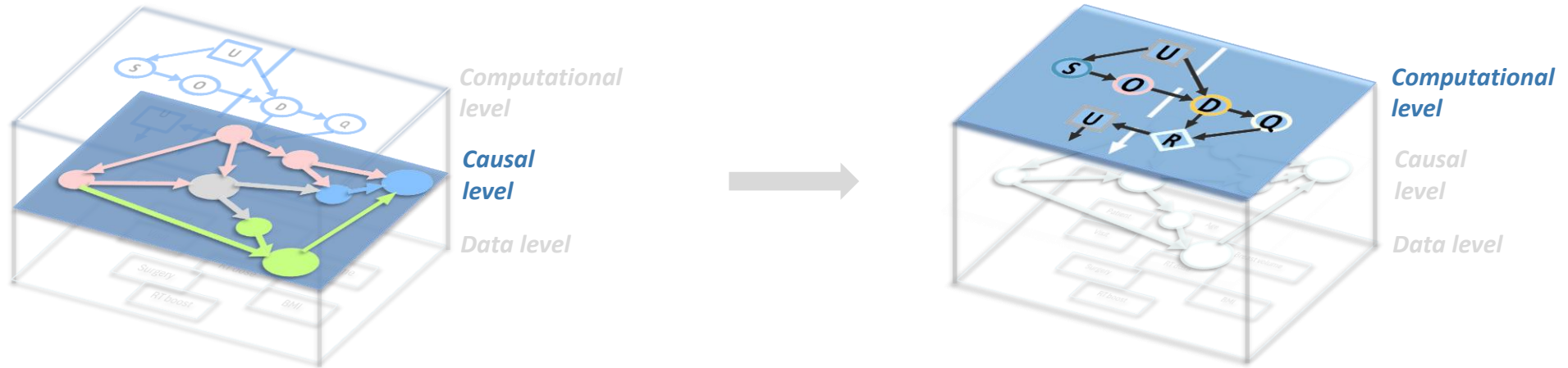
Causal level



B. Dionisi Ferrara & T. Rancati, CMON Lab, Istituto Nazionale dei Tumori



Breast cancer patients: computational level



Observed variables

$O^{pat}, O^{gen}, O^{tum}, O^{rad}$

- **Clinical data:** Age, BMI, comorbidities,...
- **Genomic data:** SNP genotypes, polygenic risk scores.
- **Imaging data:** DICOM-RT.

Control inputs/actions

U

- RT prescribed dose
- RT boost
- RT choice

Quantities of interest

E

- Effective skin radiation dose

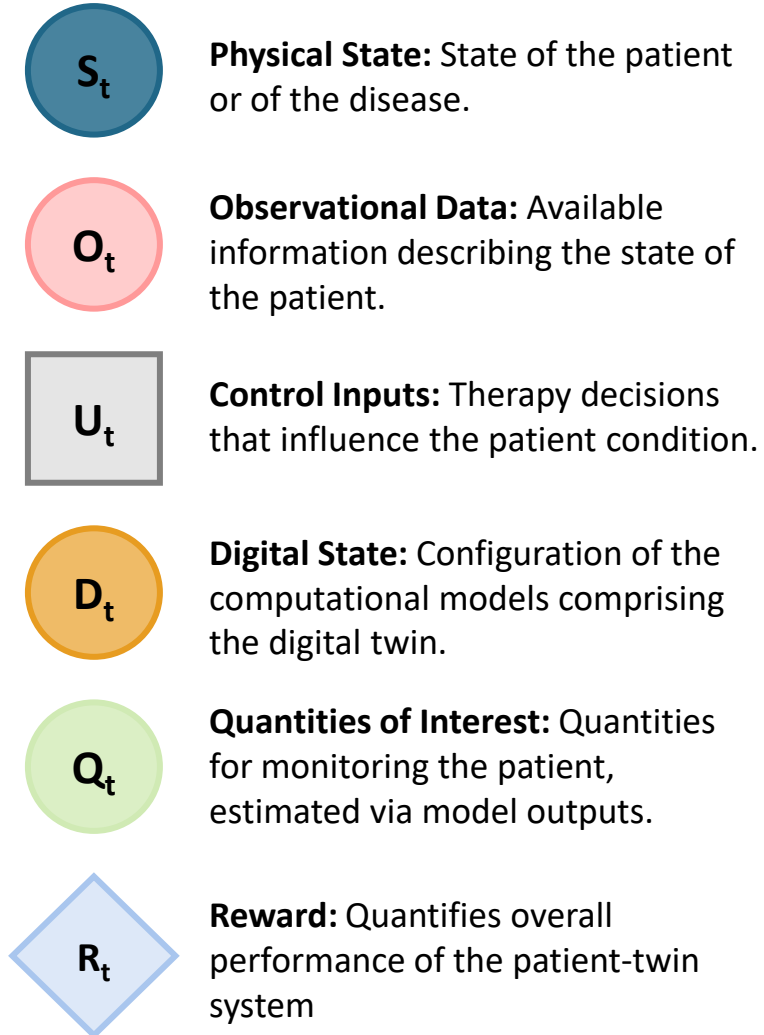
Outcome

R

- Late fibrosis

Digital Twin: PGM Overview

Semantic categories

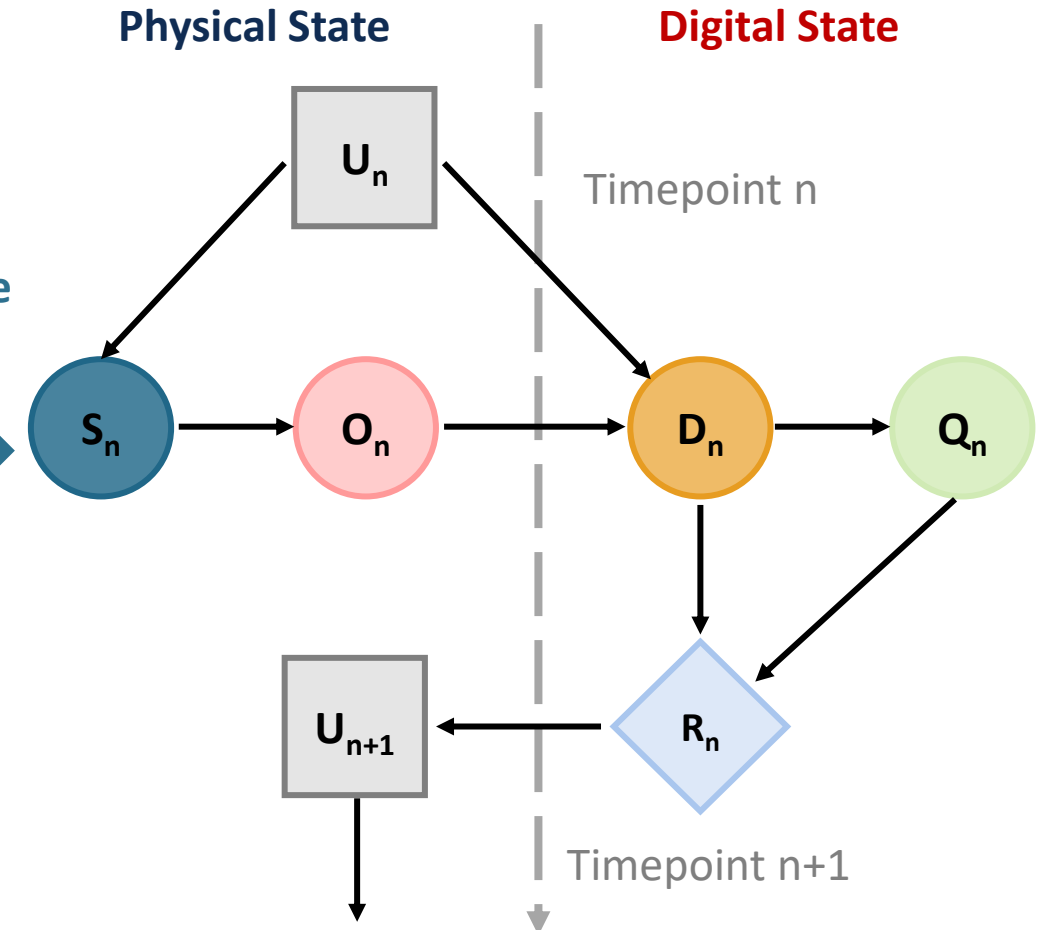


Unified representation of the
asset-twin system



Mathematical/
Computational/
Statistical model

Probabilistic Graphical Models



Kapteyn M.G., Pretorius J.V.R., Willcox K.E. A probabilistic graphical model foundation for enabling predictive digital twins at scale (2021) Nature Computational Science, 1 (5), pp. 337 - 347

Quasi-static PGM: first attempt

We design a **quasi-static decision network** that exploits patient-specific personalized treatment

- Observed variables

$O^{pat}, O^{gen}, O^{tum}, O^{rad}$

- Control inputs

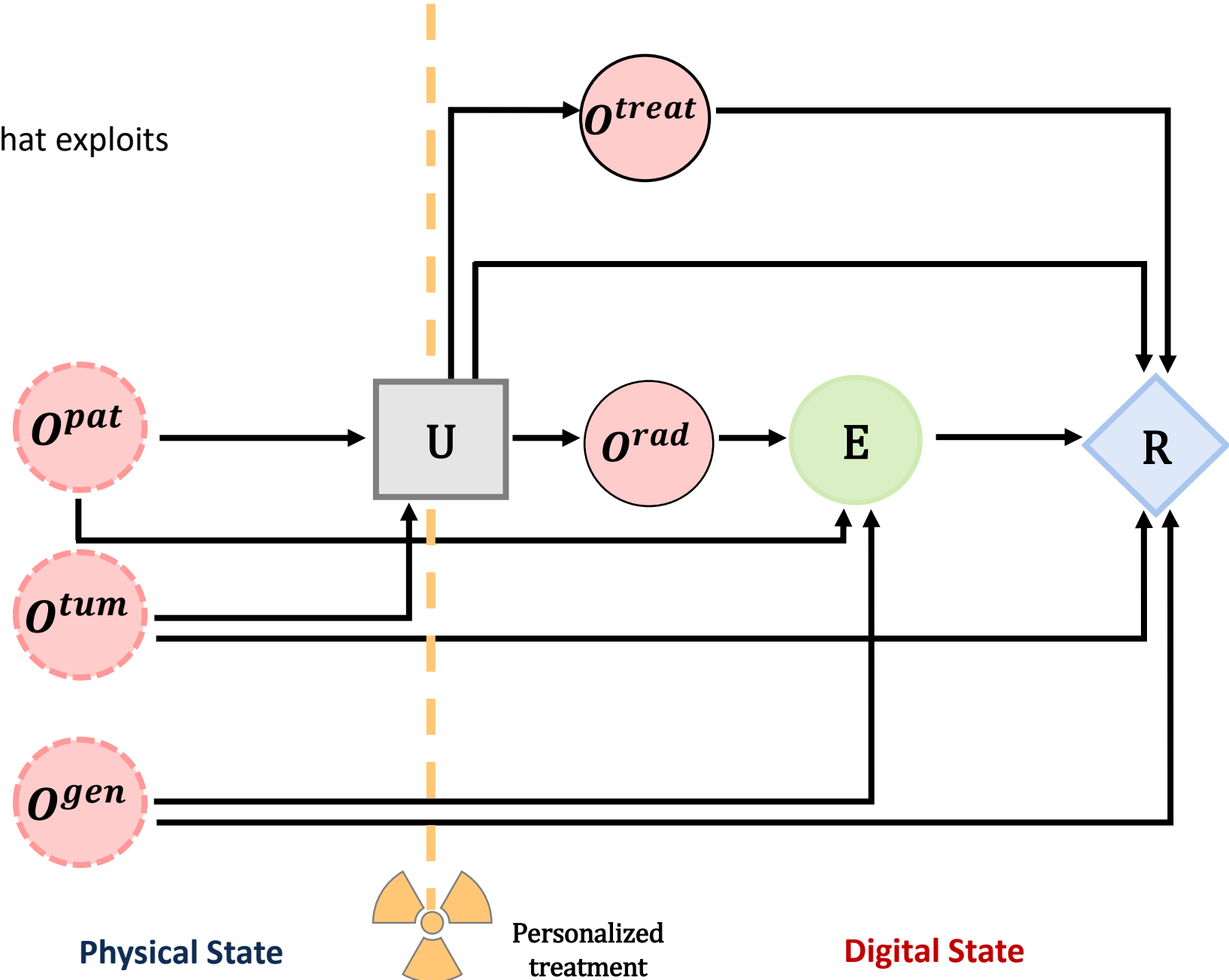
U

- Quantity of interest

E

- Outcome

R



Probabilistic approach to risk assessment

We propose a probabilistic decomposition of **late toxicity** risk into the following components.



$$O^i = O^{pat}, O^{gen}, O^{tum}, O^{rad}$$

$$\begin{aligned}
 Toxicity &= \mathbb{P}(R = 1 | E, U, O^i = o^i) \\
 &= \mathbb{P}(R = 1 | E) [\mathbb{P}(E | U) \cdot \mathbb{P}(U | o^i) + \mathbb{P}(E | o^i)] \\
 &\quad + \mathbb{P}(R = 1 | U) \cdot \mathbb{P}(U | o^i) \\
 &\quad + \mathbb{P}(R = 1 | o^i)
 \end{aligned}$$

Probabilistic modeling framework

$$\begin{aligned}
 Toxicity &= \mathbb{P}(R = 1 | E, U, O^i = o^i) & O^i &= O^{pat}, O^{gen}, O^{tum}, O^{rad} \\
 &= \mathbb{P}(R = 1 | E) [\mathbb{P}(E | U) \cdot \mathbb{P}(U | o^i) + \mathbb{P}(E | o^i)] \\
 &\quad + \mathbb{P}(R = 1 | U) \cdot \mathbb{P}(U | o^i) \\
 &\quad + \mathbb{P}(R = 1 | o^i)
 \end{aligned}$$

Using the **Beta-Bernoulli** framework we have:

Prior

Beta-Bernoulli for toxicity outcome

$$R | E, U, O^i \sim \beta(a_0(E, U, O^i), b_0(E, U, O^i))$$

- *Retrospective*
- *Population informed*

Posterior

Beta-Bernoulli for toxicity outcome

$$R | E, U, O^i \sim \beta(a_0 + \mathbb{I}[R = 1], b_0 + \mathbb{I}[R = 0])$$

- *Retrospective*
- *Population informed*

Training Data Leveraging Multi-Center Cohorts

- **Clinical covariates** (*B2a Breast patient factors baseline 2025-05-16 18-28-34.xlsx*)

$$O^{pat} = \mathbb{I}[\text{age} \geq 60 \text{ or } (\text{diabetes} + \text{hypertension} + \text{history of heart disease}) > 0]$$

- **Dosimetric covariates** (*B3 Breast clinical and treatment data form 2025-05-16 18-30-19.xlsx*)

$$E = \begin{cases} Low, & \text{if dose}_{\text{heart}} < 4\text{Gy and dose}_{\text{lung}} < 10\text{Gy} \\ Medium, & \text{otherwise} \\ High, & \text{if dose}_{\text{heart}} \geq 5\text{Gy and dose}_{\text{lung}} \geq 12.5\text{Gy} \end{cases}$$

- **Standardized toxicity outcomes (CTCAE v4.0)** (*B5 Health professional 2025-05-16 18-31.xlsx*)

$$R = \mathbb{I}[e \in \mathcal{T}_{\text{breast}} \subset \mathbb{R}^{13} : CTCAE(e) \geq 2]$$

- **Synthetic (preliminary) PRS score (proportional to toxicity risk + noise)**

$$PRS = \omega R + \varepsilon, \quad \varepsilon \sim \mathcal{N}(0, \sigma^2)$$

$$O^{gen} = \mathbb{I}[PRS > \overline{PRS}]$$



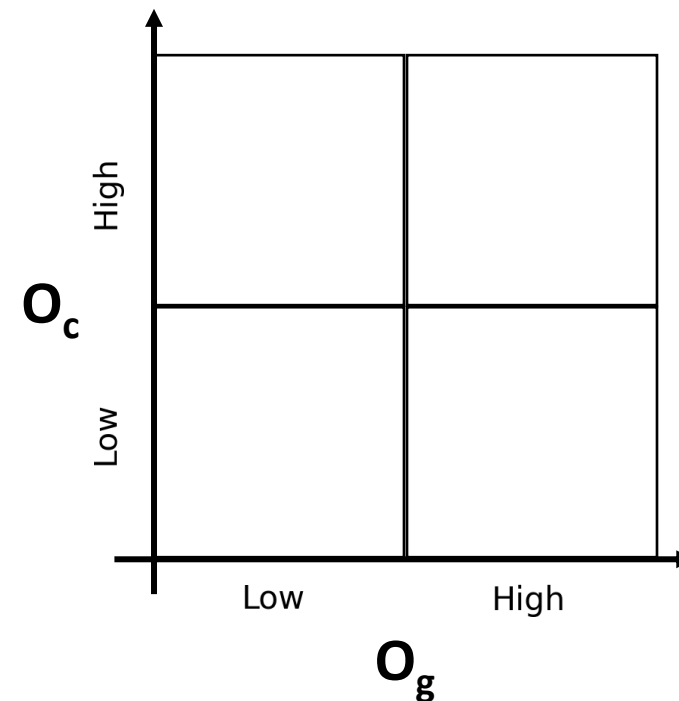
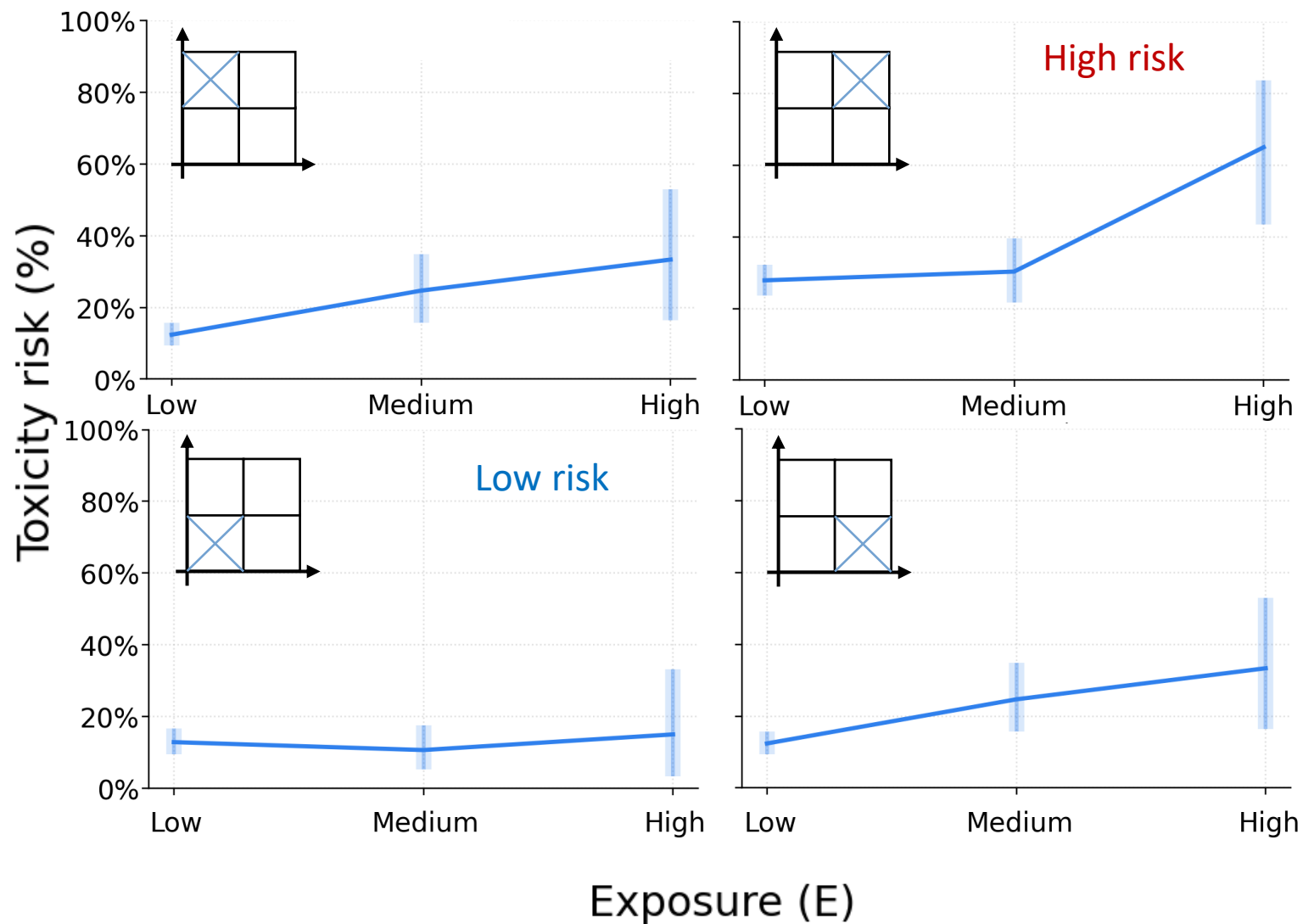
Results: toxicity table

Mean Toxicity Risk with 95% Credible Intervals

Exposure	Clinical Risk	Genomic Risk	n	Toxicity Risk (95% CI)
Low	Low	Low	325	12.8% (9.4–16.7)
Low	Low	High	287	15.9% (11.9–20.3)
Low	High	Low	434	12.4% (9.5–15.6)
Low	High	High	418	27.9% (23.7–32.2)
Medium	Low	Low	92	10.6% (5.3–17.6)
Medium	Low	High	100	26.5% (18.4–35.4)
Medium	High	Low	75	24.7% (15.8–34.8)
Medium	High	High	97	30.3% (21.7–39.7)
High	Low	Low	18	15.0% (3.4–33.1)
High	Low	High	23	36.0% (18.8–55.3)
High	High	Low	22	33.3% (16.4–52.9)
High	High	High	18	65.0% (43.5–83.7)

Results: toxicity plots

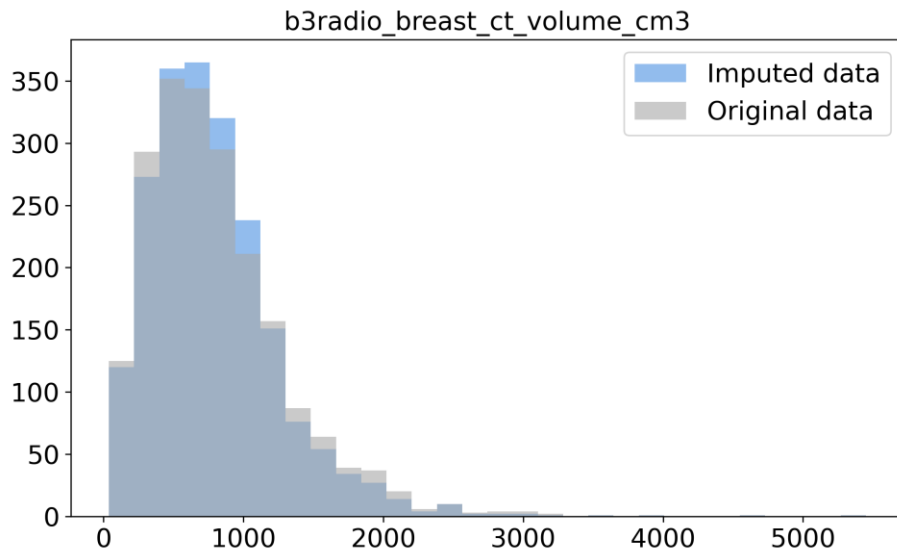
$\mathbb{P}(R = 1|E, U, O^i)$ by exposure



Next Steps in the Digital Twin Model

- **Real-time refinement** via Bayesian updates for **prior/posterior** distribution

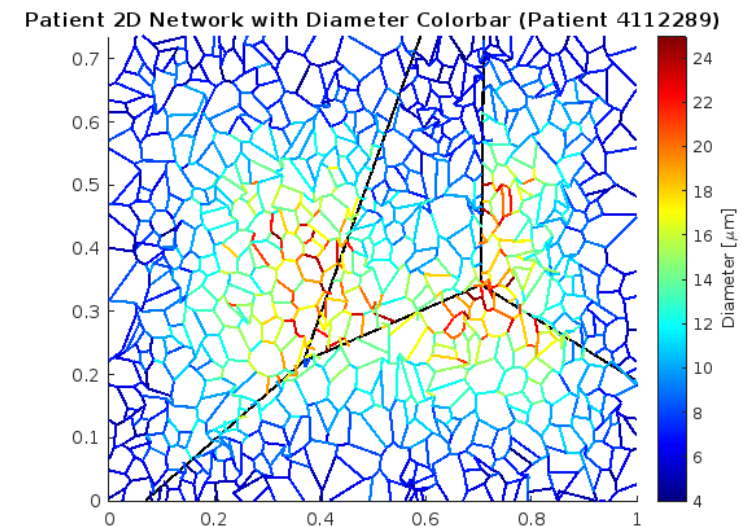
- **Imputation of missing data with Gaussian Processes**



- **Update** from quasi-static to **dynamic Digital Twin**:

$$R \rightarrow R_t$$

- **Integrate the interaction with TCP physical models for the personalized microvasculature damage**



Acknowledgments to many collaborators

Paolo Zunino and Piermario Vitullo

Politecnico di Milano



Benedetta Dionisi Ferrara and Tiziana Rancati

Istituto Nazionale Tumori



**Fondazione IRCCS
Istituto Nazionale dei Tumori**