# Physics-Based and Data-Driven-Based Algorithms for the Simulation of the Heart Function

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### the iHEART simulator

Time: 0.02 s 2





- 1.2 - 1.0 - 0.8 - 0.6

### Challenges in modeling the whole heart





### Clinical data and how we use them





I. Fumagalli, M. Fedele, C. Vergara, et al., *Computers in Biology and Medicine*, 2020 M. Salvador, M. Fedele, P. Africa, et al., *Computers in Biology and Medicine*, 2021

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Preprocessing

### The Domain Boundaries



### **Generation of cardiac fibers**



- fibers are **essential to ensure the cardiac function** (electrophysiology, active and passive mechanics)
- Laplace-Dirichlet Rule Based methods (LDRBMs)
- derived from histological observations and DT-MRI data



R. Piersanti, P. Africa, M. Fedele et al., Computer Methods in Applied Mechanics and Engineering, 2021

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reprocessing

### Transmurality





### The Electromechanics Model





### The fluid dynamics model

$$\begin{cases} -\nabla \cdot P_{ALE}(\mathbf{d}_{ALE}) = \mathbf{0} & \text{in } \widehat{\Omega} \\ \mathbf{d}_{ALE} = \mathbf{d} & \text{on } \widehat{\Sigma} \end{cases} \mathbf{u}_{ALE} = \frac{\partial \mathbf{d}_{ALE}}{\partial t} \\ \begin{cases} \rho_{f} \left[ \frac{\partial \mathbf{u}}{\partial t} + \left( (\mathbf{u} - \mathbf{u}_{ALE}) \cdot \nabla \right) \mathbf{u} \right] - \nabla \cdot \sigma_{f}(\mathbf{u}, p) = \mathbf{0} & \text{in } \Omega \\ \nabla \cdot \mathbf{u} = 0 & \text{in } \Omega \end{cases} \end{cases}$$

$$\sigma_{\rm f}(\mathbf{u},p) = \mu \left( \nabla \mathbf{u} + \nabla \mathbf{u}^T \right) - pI$$

- blood modeled as incompressible, Newtonian
- Arbitrary Lagrangian-Eulerian Navier-Stokes
- non-linear domain displacement for robustness
- VMS-LES turbulence modeling

M. Fedele, E. Faggiano, L. Dede', et al., *Biomechanics and Modeling in Mechanobiology*, 2017 A. Zingaro, I. Fumagalli, L. Dede', et al., *Discrete and Continuous Dynamical System – S*, 2022

odeling





22

### **Resistive Immersed Implicit Surface method for valves**



$$\rho_{\rm f} \left[ \frac{\partial \mathbf{u}}{\partial t} + \left( \left( \mathbf{u} - \mathbf{u}_{\rm ALE} \right) \cdot \nabla \right) \mathbf{u} \right] - \nabla \cdot \sigma_{\rm f}(\mathbf{u}, p) + \mathcal{R}(\mathbf{u}, \mathbf{u}_{\rm ALE}) = \mathbf{0} \qquad \text{in } \Omega$$
$$\mathcal{R}(\mathbf{u}, \mathbf{u}_{\rm ALE}) = \sum_{k \in \mathcal{V}} \frac{R_{\rm k}}{\varepsilon_{\rm k}} \delta_{\varepsilon_{\rm k}} \left( \varphi_{\rm k}^t(\mathbf{x}) \right) \left( \mathbf{u} - \mathbf{u}_{\rm ALE} - \mathbf{u}_{\Gamma_{\rm k}} \right)$$

 $\begin{array}{l} \varphi_{k}^{t} & \mbox{distance from valve leaflets} \\ \delta_{\varepsilon_{k}} & \mbox{smeared Dirac delta function} \\ \varepsilon_{k} & \mbox{valve half-thickness} \\ R_{k} & \mbox{penalty (resistive) coefficient} \end{array}$ 

- valve kinematics defined through  $(\varphi_k^t, \mathbf{u}_{\Gamma_k})$ :
  - pressure jump, or
  - lumped-parameter valve model
- heartbeat phases and jets and vortices induced by the valves correctly captured



M. Fedele, E. Faggiano, L. Dede', et al., *Biomechanics and Modeling in Mechanobiology*, 2017 A. Zingaro, I. Fumagalli, L. Dede', et al., *Discrete and Continuous Dynamical System – S*, 2022

### The Five Atrio-Ventricular Phases



# The cardiac perfusion model

 $\mathbf{NS}(\mathbf{u},p) = \mathbf{0}$ 





- proximal coronaries: Navier-Stokes (NS)
- intramural vessels: multi-compartment Darcy
- two-way coupling of flow rate and pressure

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Modeling

C. Michler, A.N. Cookson, R. Chabiniok et al., *International Journal of Numerical Methods in Biomedical Engineering*, 2013 S. Di Gregorio, M. Fedele, G. Pontone et al., *Journal of Computational Physics*, 2021

## Electromechanics driven CFD-Darcy model for perfusion





A. Zingaro, C. Vergara, L. Dede', F. Regazzoni, A. Quarteroni, arXiV (2023)

Modeling

• Electromechanics of the left heart

- Blood fluid dynamics in left heart and large epicardial coronaries
- Valves modeled with RIIS method
- Multicompartment Darcy model for myocardial perfusion
- One-way EM-CFD
- Fully coupled CFD-Multicompartment Darcy

### **Electromechanics driven CFD-Darcy model for perfusion**





A. Zingaro, C. Vergara, L. Dede', F. Regazzoni, A. Quarteroni, arXiV (2023)

Apr 2023

### A lumped model for the circulatory system

 $\mathbf{F}_{\text{circ}}\left(\mathbf{c}, \frac{\mathrm{d}\mathbf{c}}{\mathrm{d}t}, t\right) = \mathbf{0}$ 



#### Unknowns

c : Circulation state (pressure, flowrate, chamber volume)



- electric circuit analogy
- modular coupling with 3D models (either mechanics or fluid dynamics)



F. Regazzoni, M. Salvador, P. C. Africa, et al., Journal of Computational Physics, 2022

M. Hirschvogel, M. Bassilious, M. Jagschies, et al., Inernational Journal for Numerical Methods in Biomedical Engineering, 2017

### Numerical generation of 12-lead ECG system



M. Boulakia, S. Cazeau, M.A. Fernández, et al., *Annals of Biomedical Engineering*, 2010 E. Zappon, et al., *MOX Report*, Politecnico di Milano, 2022

Unknowns

 $v_{\rm T}$ : extra-cellular potential in torso

t = 0.000 s

0 -

-0.02 -

-0.04

-0.06

Minor inconsistencies in T-wave due to lack of ionic heterogeneity

 $\Omega_{\mathrm{torso}}$ 

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odeling

### The Integrated Mathematical Heart (the Core Equations)

$$\begin{bmatrix} \frac{\partial \mathbf{w}}{\partial t} = \mathbf{F}_{hon}^{\mathbf{w}}(v, \mathbf{w}) & \text{in } \Omega \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{w}, \mathbf{z}) & \text{in } \Omega \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{w}, \mathbf{z}) & \text{in } \Omega \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{w}, \mathbf{z}) & \text{in } \Omega \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{w}, \mathbf{z}) & \text{in } \Omega \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{w}, \mathbf{z}) & \text{in } \Omega \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{w}, \mathbf{z}) & \text{in } \Omega \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{w}, \mathbf{z}) & \text{in } \Omega \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{w}, \mathbf{z}) & \text{in } \Omega \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{w}, \mathbf{z}) & \frac{\partial SL}{\partial t} & \frac{\partial SL}{\partial t} & \text{in } \Omega \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{w}, \mathbf{z}) & \frac{\partial SL}{\partial t} & \frac{\partial SL}{\partial t} & \frac{\partial SL}{\partial t} \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{x}, \mathbf{z}) & \frac{\partial SL}{\partial t} & \frac{\partial SL}{\partial t} & \frac{\partial SL}{\partial t} \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{x}, \mathbf{z}) & \frac{\partial SL}{\partial t} & \frac{\partial SL}{\partial t} & \frac{\partial SL}{\partial t} \\ \frac{\partial z}{\partial t} = \mathbf{F}_{ion}^{\mathbf{w}}(v, \mathbf{z}) & \frac{\partial SL}{\partial t} & \frac{\partial SL}{\partial t} & \frac{\partial SL}{\partial t} & \frac{\partial SL}{\partial t} \\ \frac{\partial z}{\partial t} = \mathbf{T}_{ion}^{\mathbf{w}}(\mathbf{x}, \mathbf{z}) & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} \\ \frac{\partial z}{\partial t} = \mathbf{T}_{ion}^{\mathbf{w}}(\mathbf{x}, \mathbf{z}) & \frac{\partial z}{\partial t} \\ \frac{\partial z}{\partial t} = \mathbf{T}_{ion}^{\mathbf{w}}(\mathbf{x}, \mathbf{z}) & \frac{\partial z}{\partial t} \\ \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} \\ \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} \\ \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} \\ \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} \\ \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} \\ \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} \\ \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} \\ \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial t} & \frac{\partial z}{\partial$$

iHeart Project



### Whole heart electrophysiology





R. Piersanti, P. Africa, M. Fedele et al., Computer Methods in Applied Mechanics and Engineering, 2021

### **Results: 4CH with tuned RQD20MF + improvements**



iHeart Project



# The Displacement



### Fluid dynamics of the left heart (A.Zingaro)



Q-criterion and velocity magnitude:

- when the mitral valve opens, high speed jets coming from the LA fill the LV.
- This produces the formation of a O-ring shaped vortex, a coherent structure rolling through the leaflets of the mitral valve.
- This big vortex breaks into smaller coherent structures filling the LV and moving towards the apex.
- As the systole begins, marked by the opening of the aortic valve, the structures are flushed out in the aorta.
- At the same time, new jets are entering in the LA, but weaker with respect to the ones observed in diastole.

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### Electromechanics driven CFD-Darcy model for perfusion



A. Zingaro, C. Vergara, L. Dede', F. Regazzoni, A. Quarteroni, arXiV (2023)

1 Apr 2023



### Electromechanics driven CFD-Darcy model for perfusion





(a) electrophysiology

calcium concentration

(b)

#### A physiological simulation

velocity magnitude

 $|\boldsymbol{u}^{\mathrm{f}}|$  [m/s]

0.1 0.2 0.3 0.4

p1 [mmHg]

74.2

73.5

0.5 1.0 1.2

fluid dynamics

---- focus on epicardial coronaries

nf [mmHo]

69.1

77.0

60.4

 $p_2^p$  [mmHg]

93.4

p<sup>f</sup> [mmHg]

15.6

62.1

 $p_3^p$  [mmHg]

61.2



A. Zingaro, C. Vergara, L. Dede', F. Regazzoni, A. Quarteroni, arXiV (2023)

1 Apr 2023

(c)

perfusion

pressure

filling

### A complete simulation of a single heartbeat

Requires at least 1.7M nodes, 20M degrees of freedom for PDEs, around 31M for ODEs, 16K timesteps: in total, 700B variables for the space-time solver on 1152 cores on the supercomputer GALILEO @ CINECA



# we need a **BETTER MATH**



### For a **SUSTAINABLE WORLD**





### Learning the dynamics of active force generation





#### Accuracy

Indicator	HF-EM	ANN-EM	Relative error
Stroke volume (mL)	58.45	58.42	5.64 · 10 <sup>-4</sup>
Ejection fraction (%)	43.03	43.01	5.65 · 10 <sup>-4</sup>
Max pressure (mmHg)	112.5	112.3	2.18 · 10 <sup>-3</sup>
Work (mJ)	739.2	737.2	1.71 · 10 <sup>-3</sup>

#### Computational time (20 cores)

	lonic	Potential	Force gen.	Mechanics	Total
HF-EM	3.13 %	0.47 %	83.07 %	13.33 %	20h 18'
ANN-EM	41.21 %	4.80 %	2.54 %	51.45 %	2h' 03'

#### Memory usage

from 2198 (HF-EM) to 24 (ANN-EM) variables per nodal point

F. Regazzoni, L. Dede', A. Q., *Journal of Computational Physics*, 2019 F. Regazzoni, L. Dede', A. Q., *Computer Methods in Applied Mechanics and Engineering*, 2020

### **Multi-fidelity PINNs for the estimation of ionic parameters**





**Goal**: estimate the parameter  $\tau_{fi}$  of the Bueno-Orovio model (time constant of fast inward current) from transmembrane potential noisy measurements

### **Method**: train a **multi-fidelity PINN** minimizing a loss function weighing:

- discrepancy from a low-fidelity model (e.g. a second ANN, trained on precomputed numerical data)
- discrepancy from noisy observations
- residual of the differential equations (physicsinformed)



F. Regazzoni, S. Pagani, A. Cosenza, et al., Rendiconti Lincei Matematica e Applicazioni, 2021

### A data-driven emulator of cardiac chambers





F. Regazzoni, A. Q., Computers in Biology and Medicine, 2021

### **ANN-based surrogate of the LV electromechanical function**



training dataset

By means of model-learning, we construct a parameter space surrogate model of the LV electromechanical 150 [6Hmm] parameter space sampling × Pc function, accounting for the dependence on (training dataset generation) parameters. <sup>20</sup> م The model is trained from a set of 40 simulations obtained by sampling the parameter space. 50 100 150  $(\mathbf{p}_{\mathcal{M}}, \mathbf{p}_{\mathcal{C}})$ V<sub>LV</sub> [mL] -~~~  $p_{LV}$  [mmHg] m The testing accuracy is remarkably good (relative 100 -Model error lower than 0.01)  $\dashv\vdash$ Learning 50 testing dataset (subset) simulation  $p_1$  $V_{LV}$  [mL]  $\mathcal{M}_{\mathrm{3D}}$ - $\mathcal{C}$  $l_{\rm ANN}^{\rm single}$ - ${\cal C}$ The surrogate 125 model is reliable 100 V<sub>LV</sub> plv [mmHg]  $\mathbf{p}_{\mathcal{M}}$ also for longer 75 time-horizons than  $\mathcal{M}_{3D}$ those considered in  $\mathcal{M}_{3D}$ - $\mathcal{C}$ the training set!  $\mathcal{M}_{\mathsf{ANN}}$ 12010014060 80 160 $V_{\rm LV}$  [mL]

F. Regazzoni, L. Dede', A. Q., Journal of Computational Physics, 2019

F. Regazzoni, M. Salvador, L. Dede', A. Q., Computer Methods in Applied Mechanics and Engineering, 2022

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 $p_{LV}$ 

### ANN-based surrogate model for global sensitivity analysis



F. Regazzoni, L. Dede', A. Q., Journal of Computational Physics, 2019

F. Regazzoni, M. Salvador, L. Dede', A. Q., Computer Methods in Applied Mechanics and Engineering, 2022

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algorithms

 $\overline{\triangleleft}$ 

<sup>2</sup>hysics-driven meet

### **ANN-based surrogate model for Bayesian parameter estimation**





F. Regazzoni, L. Dede', A. Q., Journal of Computational Physics, 2019

F. Regazzoni, M. Salvador, L. Dede', A. Q., Computer Methods in Applied Mechanics and Engineering, 2022

### **DL-enhanced physics-based ROMs for cardiac mechanics**



### Full order: finite element method

- high fidelity
- many degrees of freedom ×
- computationally demanding imes

### Galerkin ROM: projection on linear space

- physics-based
- still depends on high-fidelity dimension ×

# **Deep-HyROMnet:** Galerkin-ROM with ANN approximation of non-linear operators

- physics-based
- independent of high-fidelity dimension

L. Cicci, S. Fresca, S. Pagani et al., *Mathematics in Engineering*, 2022 L. Cicci, S. Fresca, A. Manzoni, *Journal of Scientific Computing*, 2022 (accepted)



# Physics-aware NN for inverse problems in electrophysiology

**Goal**: reconstruct the ventricles electrical activity from non-invasive recordings of the body surface potential (inverse problem of electrocardiography)



**Method**: train a physics-aware Neural Network (autoencoder) characterized by:

- Physical awareness (I): a projection based reduced-order model efficiently encodes the "forward map"
- Generalization: model performs well also in small data regimes.



**Results**: the physics-aware NNs reconstruct activation maps with a 4% mean relative error, requiring only 10 minutes training on a regular laptop

R. Tenderini, S. Pagani, S. Deparis, A. Q., SIAM Journal on Scientific Computing, 2022

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Physics-driven meet AI algorithms



# **Atrial fibrillation (AF)**



### Clinical question: which are the mechanisms behind AF progression?



- slow conduction corridors and pivot points quantitatively characterize AF progression
- Numerical simulations confirm the role of slow conduction corridors in AF sustainment (localized reentry anchoring)

A. Frontera, S. Pagani, L.R. Limite et al., *JACC: Clinical Electrophysiology*, 2022 S. Pagani, L. Dede', A. Frontera et al., *Frontiers in Physiology*, 2021

# Ventricular tachycardia





# Ventricular tachycardia and fibrillation



(/m/)

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JOHNS HOPKINS

NIVERSITY

Clinical question: are ventricular tachycardia and fibrillation better simulated by accounting for mechanical deformation?



From electrophysiology to electromechanics (geometry-mediated mechano-electric feedbacks and stretch-activated channels)

# **Electrophysiology** and **electromechanics** simulations may differ in **conduction velocity**, **electric stability** and **hemodynamic stability**

M. Salvador, M. Fedele, P.C. Africa et al., *Computers in Biology and Medicine*, 2021 M. Salvador, F. Regazzoni, S. Pagani et al., *Computers in Biology and Medicine*, 2022

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Simulation

# Hypertrophic Cardiomyopathy (HCM)





I. Fumagalli, M. Fedele, C. Vergara, et al., *Computers in Biology and Medicine*, 2020 I. Fumagalli, P. Vitullo, C. Vergara, et al., *Frontiers in Physiology*, 2022

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# **Transcatheter Aortic Valve Implantation (TAVI)**





- Analysis based on pre-implantation data only
- WSS stronger and more persistent in SVD cases
- η index discriminating SVD from NO-SVD, based on Time-Averaged WSS (TAWSS) Critical Area (CA):

$$\eta = \frac{|CA|}{|\Gamma_{\text{wall}}|}, \text{ with } CA = \{ \mathbf{x} \in \Gamma_{\text{wall}} \colon TAWSS(\mathbf{x}) > 0.5 \text{Pa} \}$$

I. Fumagalli, R. Polidori, F. Renzi et al., MOX Report, Politecnico di Milano, 2022

## Estimating cardiac blood flow maps





Clinical question: can we replace CT scans and stress protocols with a computational estimation of myocardial blood flow maps?



Adenosine

injection

Simulation

### **Clinical pipeline**



### Stress-CTP scan

# MBF maps

**Consistency tests**: calibration of **perfusion model** on available maps yields **excellent agreement** 

**Ongoing:** calibration of patient-specific models based on **pressure data only** (no maps)



S. Di Gregorio, C. Vergara, G. Montino Pelagi et al., European Journal of Nuclear Medicine and Molecular Imaging 2022

## Transcatheter Aortic Valve Implantation (TAVI)



I. Fumagalli, R. Polidori, F. Renzi et al., *Int J Num Meth Biomed Eng*, 2023 Alfio Quarteroni

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